# Hierarchical DAG scheduling for Hybrid Distributed Systems

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#### **Outline**

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  - Multiple CUDA Streams
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- Performance Evaluation
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- Conclusions

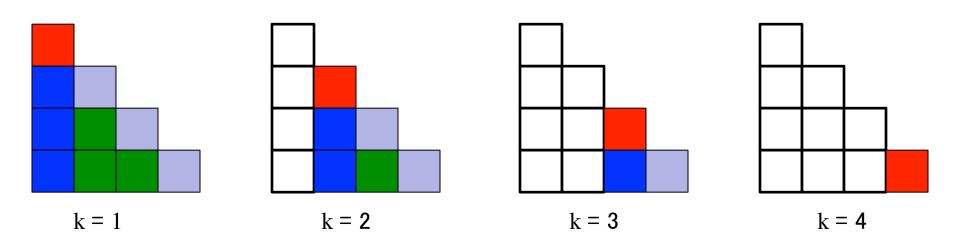
#### Introduction

- Different optimal task granularity on GPU and CPU
- "Hierarchical DAG"
  - Adapt the granularity of tasks dynamically according to execution location.
- Linear algebra application (matrix factorization).
  - Tiled algorithm. Tile size is a critical tuning parameter
  - "Hierarchical DAG" allows different tile sizes coexist during execution

#### **Background Matrix Factorization**

Diagonal matrix: Cholesky

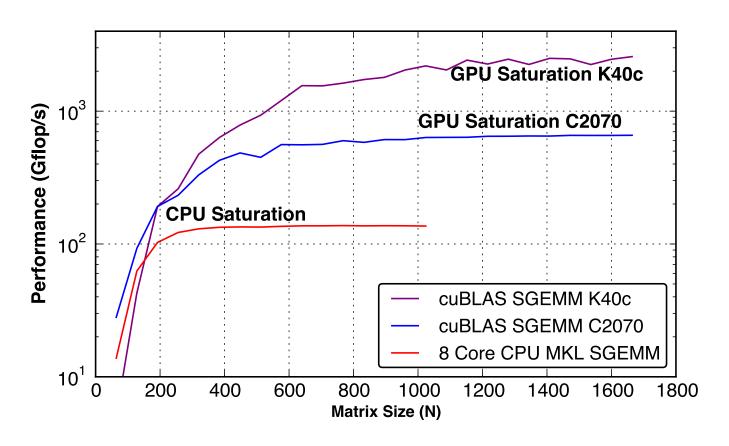
Square matrix: QR



Example of Cholesky factorization on  $4 \times 4$  matrix

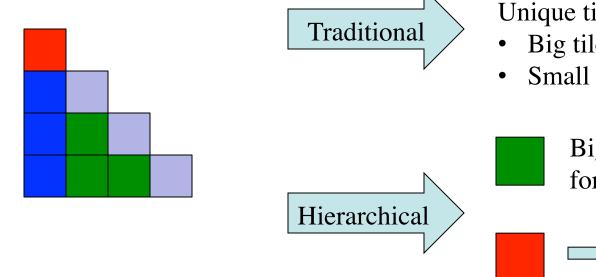


#### **Motivation**



Impact of the problem granularity on the performance of the CPU and GPU SGEMM compute kernel when applied to a single tile of size N.

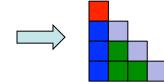
#### Motivation (cont'd)



Unique tile size for each task

- Big tile size: not enough parallelism
- Small tile size: less GPU occupancy



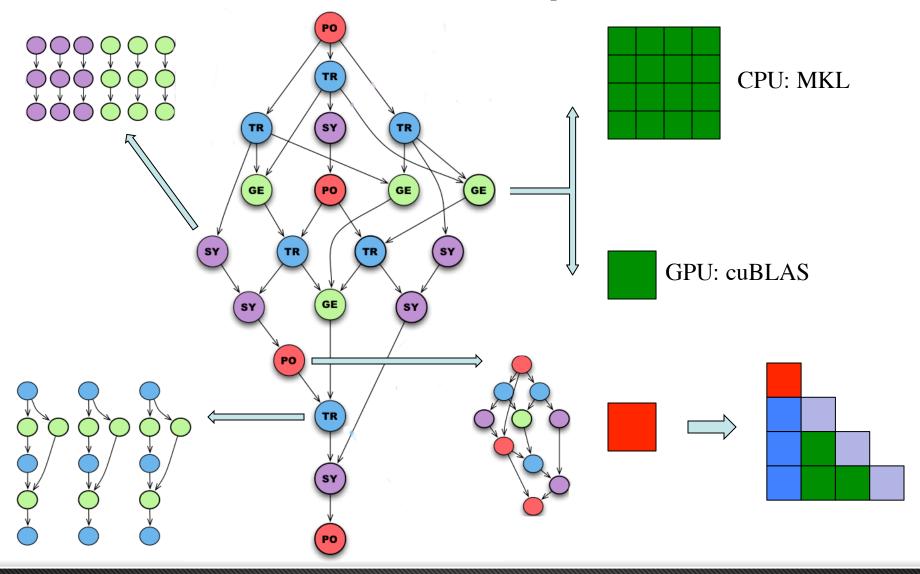


Small tile size on CPU to expose more parallelism





#### **Hierarchical DAG Implementation**

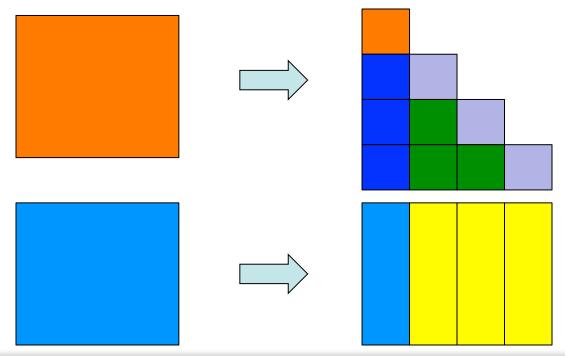


## Hierarchical DAG Implementation (cont'd)

- Coarse grain DAG
  - Creation operation is collective across the entire distributed memory domain.
  - Unique global identifier
- > Fine grain DAG
  - Creation operation is dynamic, depending on data locality and work load of devices.
  - No global identifier, visible only to local node

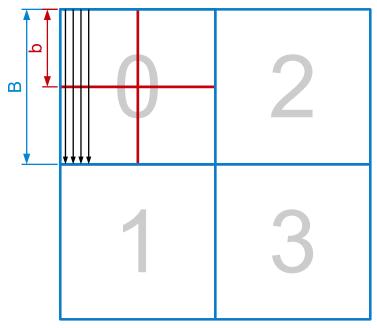
#### **Hierarchical DAG LA Applications**

- Generic solution can be applied to any algorithm that tasks can be split.
  - Cholesky factorization: fine grain tasks operating on small square tiles.
  - QR factorization: fine grain tasks operating on small rectangle tiles.



#### **Hybrid Data Layout**

- Different data layout: tile and LAPACK
- For sub-tiles in the fine grain DAG (red), the data layout is the same as the LAPACK layout with interleaved data, while tile layout (blue) is used for large tiles and permits a much more efficient data transfer to/from the accelerators



#### **Hierarchical DAG Support in PaRSEC**

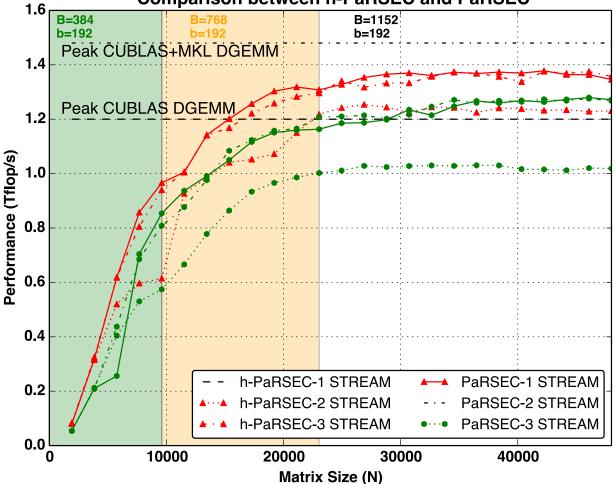
- Tasks can be executed on either CPU or GPUs if both implementations are provided.
- > Tasks will be split dynamically to provide more parallelism if current parallelism is not sufficient.
- Multiple CUDA streams for better GPU occupancy.
- Multi-level GPU task queues for dynamic task execution order.
- Dynamic CPU/GPU load balance
- CPU/GPU data coherence protocol for minimal data movement.

#### **Multiple CUDA Streams**

- Define GPU task as three stages:
  - Move data into GPU
  - Kernel execution
  - Move data out of GPU
- Data move in/out
  - Each direction takes one CUDA stream.
  - Data prefetch
- Kernel execution: multiple CUDA streams depending on GPU generations

#### Multiple CUDA Stream (cont'd)

Hybrid DPOTRF on Bunsen (16 cores CPU and 1 k40c GPUs)
Comparison between h-PaRSEC and PaRSEC



Performance difference between hierarchical DAG and the standard version on POTRF with a varying number of CUDA streams

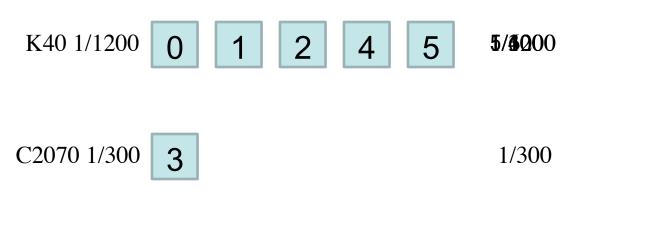
#### **Multi-level GPU Task Queues**

- Each stage of GPU task contain a queue.
- Out of order task execution
  - Task priority: promote the execution of tasks which have higher priority
  - Data availability: promote the execution of tasks for which a copy of the data is already available
- CUDA events track the completion of each stage.

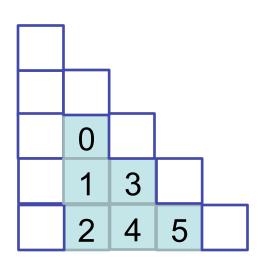
#### **CPU/GPU Dynamic Load Balance**

- Task weight: the inverse of the peak performance of the kernel on the device
- Coarse grain DAG
  - Workload: task will be assigned to the device which would have the lowest workload if this task runs on it.
  - Locality: if a task whose R&W data is already on a device, then later tasks which use the same R&W data will stay on this device. This does not apply to CPU.
- Fine grain DAG
  - Job stealing

#### CPU/GPU Load Balance (cont'd)

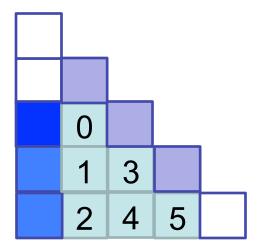


CPU 1/19

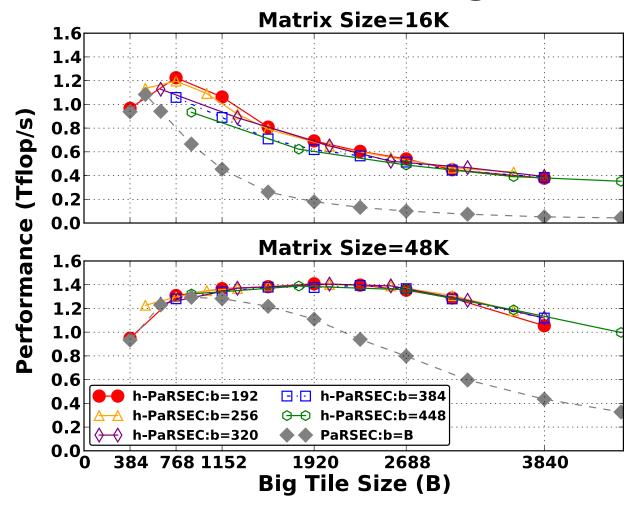


#### Data Coherence between CPU & GPU

- Modified MOESI protocol
  - Read Only, Write Only, Read Write
  - Owner of data
  - Number of readers
  - Location of data on each device
- Out of Core GPU Operations
  - Write LRU and Read Only LRU
  - Clean up the Write LRU when GPU dedicated thread is idle.
  - Improve Load Balance.

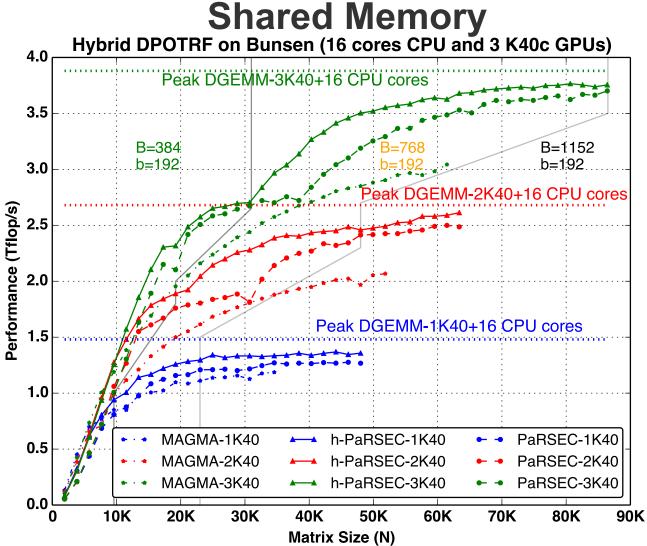


### Performance Evaluation Tile Size Tuning



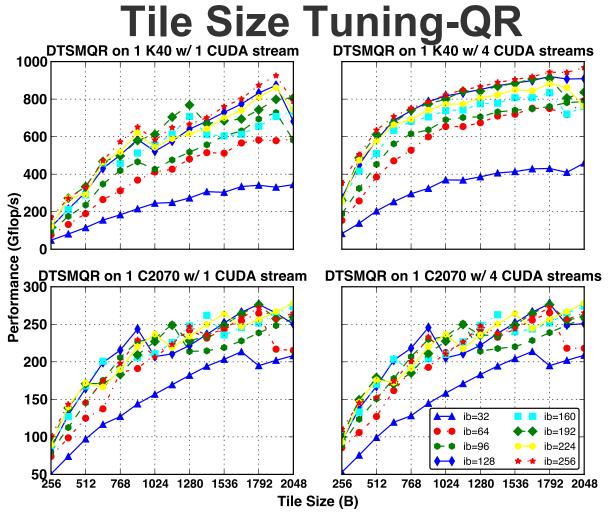
Performance for different tile size parameters (DPOTRF, using 1 GPU on Bunsen)

### **Performance Evaluation**



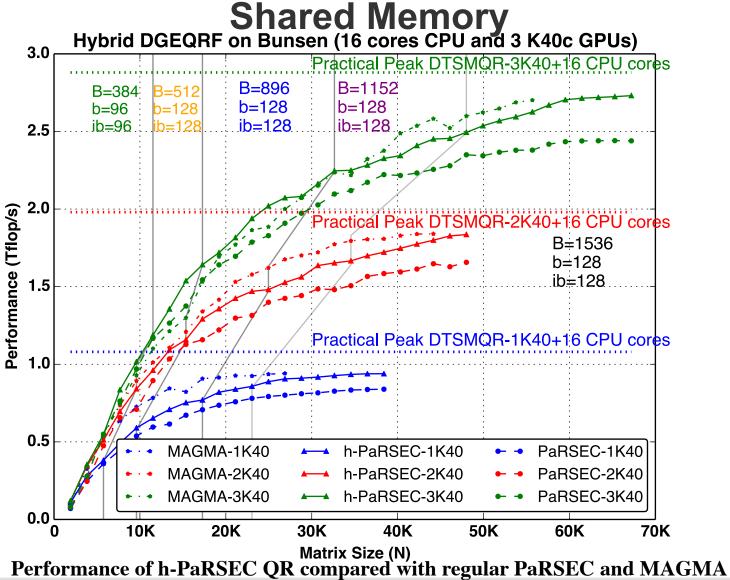
Performance of h-PaRSEC Cholesky compared with regular PaRSEC and MAGMA

### Performance Evaluation Tile Size Tuning-QR



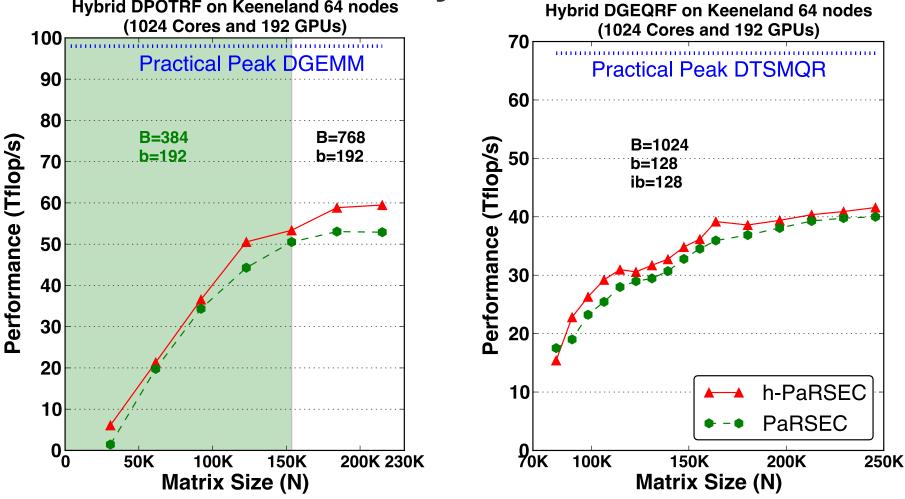
Performance of DTSMQR kernel on Fermi C2070 and Kepler K40 with 1 and 4 CUDA streams.

#### **Performance Evaluation**



#### **Performance Evaluation**

Distributed Memory - Performance Scale
Hybrid DPOTRF on Keeneland 64 nodes
Hybrid DGFORF on Keeneland 64 nodes



DPOTRF and DGEQRF performance with varying problem size; the dotted line is the DGEMM/DTSMQR peak performance (on 1 node, multiplied by 64)

### Performance Evaluation Distributed Memory – Weak Scale

Hybrid DPOTRF/DGEQRF Weak Scaling on Keeneland 64 nodes (1024 cores and 192 GPUs) 1.6 Practical Peak DGEMM 1.4 per Node Practical Peak DTSMQR 0.8 .flop/s 0.6 DPOTRF(h-PaRSEC) DGEQRF(h-PaRSEC) 0.2 DPOTRF(PaRSEC) ▲ → DGEQRF(PaRSEC) 16 32 36 48 64 No. of Nodes

Weak Scalability: DPOTRF and DGEQRF performance as a function of the number of nodes, with a problem size scaled accordingly

(Keeneland, 3 M2090 GPUs and 16 cores per node)

#### **Conclusions**

- Proposed a "hierarchical DAG" approach that is able to adjust granularity of tasks depending on the type of resources where it will be executed
- From various performance evaluation, it is demonstrated that "hierarchical DAG" approach is able to improves the asymptotic performance for large matrices by employing the appropriate task grain on accelerators, while retaining a suitable amount of parallelism for CPU computations. It also enhances the scalability of the underlying algorithms.